



# C. U. SHAH UNIVERSITY WADHWAN CITY FACULTY OF SCIENCES

**B.Sc.** 

SEM - IV

Syllabi (CBCS) of Mathematics



## **FACULTY OF SCIENCES**

## **DEPARTMENT OF MATHEMATICS**

**SEMESTER: IV** 

#### COURSE: B.Sc. SUBJECT NAME: Differential and Integral Calculus SUBJECT CODE: 4SC04DIC1 Teaching & Evaluation Scheme:-

| Теа | ching  | hours | /week | Credit | Evaluation Scheme/semester |  |        |            |                |    |  |     |
|-----|--------|-------|-------|--------|----------------------------|--|--------|------------|----------------|----|--|-----|
|     | Theory |       |       |        |                            |  | Practi |            |                |    |  |     |
| Th  | Tu     | Pr    | Total |        |                            | Sessional University<br>Exam Exam Internal |        | University | Total<br>Marks |    |  |     |
|     |        |       |       |        | Marks                      | Hrs  | Marks  | Hrs        | Pr             | τw |  |     |
| 3   | 0      | 0     | 3     | 3      | 30                         | 1.5  | 70     | 3          |                |    |  | 100 |

**Objectives:** - The main objectives of this course are to study gradient, divergence curl, ILine integral, surface integral and to study theorems related to them.

**Prerequisites:-**Knowledge of differentiation, integration and basic calculus.

| Sr. | Course Contents   | Hours |  |  |  |  |  |
|-----|---|-------|--|--|--|--|--|
| No. |   |       |  |  |  |  |  |
| 1   | First order partial differential equation, Formation of partial differential equation, Linear equations of first order.                         | 5     |  |  |  |  |  |
| 2   | Curves, Surfaces, Differentiation along a curve, Applications to geometry: Curvature in Cartesian and polar co-ordinates                        |       |  |  |  |  |  |
|     | Singular points for plane curves especially points of inflection and double points.   | 8     |  |  |  |  |  |
| 3   | Equations of Tangent and normal to the curves, Tangent plane and normal line to the surfaces, Gradient, Divergence and Curl of vectors.         | 8     |  |  |  |  |  |
| 4   | Double integral, Change of order, Triple integral, Change of variable in multiple integral.   | 12    |  |  |  |  |  |
| 5   | Line integral, Surface integral, Green's theorem, Gauss – Divergence<br>theorem, Stoke's theorem (Without proof), Examples based on<br>theorems | 12    |  |  |  |  |  |



**Learning Outcomes:**-After successful completion of this course students will be able to solve any problem related to differential and integral calculus.

#### **Books Recommended:-**

- 1. 'Differential Calculus', Shanti Narayan & P. K. Mittal, S. Chand.
- 2. 'Integral Calculus', Shanti Narayan & P. K. Mittal, S. Chand.
- 3. 'Advanced Calculus', David Widder, Prentice hall, New Delhi.
- 4. 'Advanced Calculus Volume-II, T. M. Apostol, Blaisdoll.
- 5. 'Partial Differential Equation', **T. Amarnath**, *Narosa*.
- 6. 'Calculus', James Stewart, *Brooks/Cole publishing company*.
- 7. 'Applied Calculus', S. T. Tan, Brooks/Cole publishing company.

- 1. <u>http://math.stackexchange.com/questions/523074/differential-calculus-vs-integral-calculus</u>
- 2. <u>https://www.khanacademy.org/math/multivariable-</u> <u>calculus/line\_integrals\_topic/greens\_theorem/v/green-s-theorem-example-1</u>
- 3. <u>http://www.math24.net/greens-formula.html</u>
- 4. <u>http://www.math24.net/stokes-theorem.html</u>
- 5. <u>http://youtube.com/watch?v=W0u0AVa-xig</u>
- 6. <u>http://mathinsight.org/triple\_integral\_examples</u>
- 7. <u>http://mathinsight.org/triple\_integral\_introduction</u>



## FACULTY OF SCIENCES

## **DEPARTMENT OF MATHEMATICS**

#### COURSE: B.Sc. SUBJECT NAME: Linear Algebra-II Teaching & Evaluation Scheme:-

#### SEMESTER: IV SUBJECT CODE: 4SC04LIA1

| Теа | ching | hours | /week | Credit | Evaluation Scheme/semester        |     |          |     |            |                |     |     |
|-----|-------|-------|-------|--------|-----------------------------------|-----|----------|-----|------------|----------------|-----|-----|
|     |       |       |       |        | Theory                            |     |          |     |            | Practi         | cal |     |
| Th  | Tu    | Pr    | Total |        | Sessional University<br>Exam Exam |     | Internal |     | University | Total<br>Marks |     |     |
|     |       |       |       |        | Marks                             | Hrs | Marks    | Hrs | Pr         | TW             |     |     |
| 3   | 0     | 0     | 3     | 3      | 30                                | 1.5 | 70       | 3   |            |                |     | 100 |

**Objectives: -** The main objectives of this course are

- To provide students with a good understanding of the concepts and methods of linear algebra
- To help the students develop the ability to solve problems using linear algebra.
- To connect linear algebra to other fields both within and without mathematics.

#### **Prerequisites:-**

Students must be familiar with the properties of set theory, function, Determinant and Matrices. Students should have basic knowledge of vector calculus.

| Sr. | Course Contents   | Hours |
|-----|---|-------|
| No. |   |       |
| 1   | Orthogonality, Geometrical application, orthogonal projection onto a    | 9     |
|     | line, orthonormal basis, orthogonal complements and projections.        | 9     |
| 2   | Linear functionals and hyper-planes, orthogonal transformations,        | 9     |
|     | associated co-ordinates, reflections, orthogonal map of the plane.      | 9     |
| 3   | Determinants and its properties, Value of a determinant, Basic results- |       |
|     | Laplace expansion, Cramer's rule, Application to geometry, orientation  | 9     |
|     | and vector product.   |       |



| 4 | Rotation of axes of conics, Review Eigenvalues and eigenvectors,         | ٥ |  |  |  |  |  |  |  |  |
|---|--|---|--|--|--|--|--|--|--|--|
|   | Diagonalization of symmetric matrices.                                   |   |  |  |  |  |  |  |  |  |
| 5 | Conics and quadrics, classification of Quadrics, computational examples. | 9 |  |  |  |  |  |  |  |  |

#### Learning Outcomes:-

- Analyze real world scenarios to recognize when vectors, matrices, or linear systems are appropriate, formulate problems about the scenarios, creatively model these scenarios
- Work with vectors, matrices, or linear systems symbolically and geometrically in various situations
- Give examples and non-examples of linear transformations, evaluate the matrix representations of a linear transformation

#### **Books Recommended:-**

- 1. 'Linear Algebra A Geometric Approach', S. Kumaresan, Prentice Hall, New Delhi.
- 2. 'Finite Dimensional Vector spaces', **P. Halmos,** *Literary Licensing, LLC.*
- 3. 'Matrix and Linear algebra', K. B. Dutta, Prentice Hall, New Delhi.
- 4. 'Linear Algebra-A problem book', P. R. Halmos, Cambridge university Press.
- 5. 'Linear Algebra', **G. Paria**, New central book agency-Calcutta.
- 6. 'Linear algebra and applications', Gilbert Strang Thomson, Cole publishing company.

- 1. <u>http://www.math.clarku.edu/~djoyce/ma130/vectorspace.pdf</u>
- 2. http://www.saylor.org/courses/ma211/
- 3. <u>http://en.wikipedia.org/wiki/Linear\_algebra</u>
- 4. <u>https://www.khanacademy.org/math/linear-algebra</u>



## FACULTY OF SCIENCES

## **DEPARTMENT OF MATHEMATICS**

#### COURSE: B.Sc. SUBJECT NAME: Numerical Methods Teaching & Evaluation Scheme:-

#### SEMESTER: IV SUBJECT CODE: 4SC04NUM1

| Теа | ching | hours | /week | Credit | Evaluation Scheme/semester        |     |          |     |            |                |  |     |
|-----|-------|-------|-------|--------|-----------------------------------|-----|----------|-----|------------|----------------|--|-----|
|     |       |       |       |        | Theory                            |     |          |     |            | cal            |  |     |
| Th  | Tu    | Pr    | Total |        | Sessional University<br>Exam Exam |     | Internal |     | University | Total<br>Marks |  |     |
|     |       |       |       |        | Marks                             | Hrs | Marks    | Hrs | Pr         | TW             |  |     |
| 3   | 0     | 0     | 3     | 3      | 30                                | 1.5 | 70       | 3   |            |                |  | 100 |

**Objectives:** -The main objectives of this course are

- Find the Lagrange Interpolation Polynomial for any given set of points.
- Use finite differences for interpolation, differentiation, etc.

#### **Prerequisites:-**

Basic knowledge of Linear Algebra and differential equations.

| Sr. | Course Contents  | Hours |
|-----|--|-------|
| No. |  |       |
| 1   | Estimation of error in differentiation formula based on Newton's     | 9     |
|     | forward and backward formulae, and Stirling's formula.               | 9     |
| 2   | Differentiation formulae of un-equispaced arguments, General         | 9     |
|     | quadrature formula, Trapezoidal rule, Simpson's rule, Weddel's rule. | 9     |
| 3   | Quadrature formula based on Lagrange's formula, Newton-Cotes         |       |
|     | formula, Numerical integration formula based on central difference   | 9     |
|     | formulae, Euler-Maclaurin sum formula.                               |       |
| 4   | Algebraic and transcendental equations, Numerical solution of        |       |
|     | differential equations of first order; Graphical method, method of   | 9     |
|     | bisection, method of iteration, Newton-Raphson formula, Newton's     | 9     |
|     | iterative formula, method of false position.                         |       |



| 5 | Euler's method, Euler's modified method, Picard's method.   | 0 |
|---|---|---|
|   | Taylor's series method, Runge-Kutta method, Milne's method. | 9 |

#### Learning Outcomes:-

After successful completion of this course students will be able to

- Analyze errors and have an understanding of error estimation.
- Be able to use polynomials in several ways to approximate both functions and data, and to match the type of polynomial approximation to a given type of problem.
- Be able to solve equations in one unknown real variable using iterative methods and to understand how long these methods take to converge to a solution.
- Derive formulas to approximate the derivative of a function at a point, and formulas to compute the definite integral of a function of one or more variables.
- Choose and apply any of several modern methods for solving systems of initial value problems based on properties of the problem.

#### **Books Recommended:-**

- 1. 'Numerical Analysis and Computational Procedures', **S. A. Moolah**,*New Central Book Agency (P) Ltd., Calcutta.*
- 2. 'Elementary Numerical analysis', S. S. Sastry, Prentice Hall, New Delhi.
- 3. 'Numerical mathematical analysis 6<sup>th</sup> edition', **Scarborough**, *Oxford& IBH*.
- 4. 'Numerical analysis', **S.Kunz,** *Mcgraw Hill Book New York.*
- 5. 'Numerical Analysis', **Richard Burden and J. Douglas Thomson,** *Cole Pub Co; 6th edition* (*December 24, 1996*)

- 1. <u>http://mathfaculty.fullerton.edu/mathews/numerical.html</u>
- 2. <u>http://en.wikipedia.org/wiki/Numerical analysis</u>
- 3. <u>http://ocw.mit.edu/courses/mathematics/18-330-introduction-to-numerical-analysis-spring-2012/</u>
- 4. http://math.mercyhurst.edu/~platte/syllabi/numerical analysis spring 09 10.html



## FACULTY OF SCIENCES

## **DEPARTMENT OF MATHEMATICS**

#### COURSE: B.Sc. SUBJECT NAME: Mathematical Finance

#### SEMESTER: IV SUBJECT CODE: 4SC04MAF1

#### **Teaching & Evaluation Scheme:-**

| Теа | ching | hours | /week | Credit | Evaluation Scheme/semester |     |                |     |           |    |            |                |
|-----|-------|-------|-------|--------|----------------------------|-----|----------------|-----|-----------|----|------------|----------------|
|     |       |       |       |        |                            | The | ory            |     | Practical |    |            |                |
| Th  | Tu    | Pr    | Total |        | Sessio<br>Exan             | -   | Univer<br>Exar | •   | Internal  |    | University | Total<br>Marks |
|     |       |       |       |        | Marks                      | Hrs | Marks          | Hrs | Pr        | τw |            |                |
| 3   | 0     | 0     | 3     | 3      | 30                         | 1.5 | 70             | 3   |           |    |            | 100            |

Objectives: - The main objectives of this course are

- To understand the growth of market value and the variabeles depenging upon .
- To formulate profit and loss as mathematical tool.
- To understand the portfolio diagram with different models like Markowitz model.

**Prerequisites:-** Students must be familiar with the properties of set function, Derivative ,integration etc. and basic techniques of numerical methods and statistics.

#### **Course outline:-**

| Sr. | Course Contents   | Hours |  |  |  |  |  |  |  |
|-----|---|-------|--|--|--|--|--|--|--|
| No. |   |       |  |  |  |  |  |  |  |
| 1   | Basic principles: Comparison, arbitrage and risk aversion, Interest (simple | 9     |  |  |  |  |  |  |  |
|     | and compound, discrete and continuous).                                     |       |  |  |  |  |  |  |  |
| 2   | Time value of money, inflation, net present value, internal rate of return  |       |  |  |  |  |  |  |  |
|     | (calculation by bisection and Newton-Raphson methods).                      |       |  |  |  |  |  |  |  |
| 3   | Comparison of NPV and IRR. Bonds, bond prices and yields. Floating-rate     | 9     |  |  |  |  |  |  |  |
|     | bonds, immunization.  |       |  |  |  |  |  |  |  |
| 4   | Asset return, short selling, portfolio return, (brief introduction to       | 9     |  |  |  |  |  |  |  |
|     | expectation, variance, covariance and correlation),                         |       |  |  |  |  |  |  |  |

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| 5 | Random returns, portfolio mean return and variance, diversification, | 9 |
|---|--|---|
|   | portfolio diagram, feasible set, Markowitz model (review of Lagrange |   |
|   | multipliers for 1 and 2 constraints).                                |   |

Learning Outcomes:- After the successful completion of the course, students will be able to

- Understand the growth of market value and the variables depending upon.
- Formulate profit and loss as mathematical tool.
- Understand the portfolio diagram with different models like Markowitz mode

#### **Books Recommended:-**

- 1. 'Investment Science', D. G. Luenberger, Oxford University Press, Delhi, 1998.
- 2. 'Options, Futures and Other Derivatives', J. C. Hull, Prentice-Hall India, Indian reprint, 2006.
- 3. 'An Elementary Introduction to Mathematical Finance', **S. Ross,** *Cambridge University Press, USA, 2003.*

- 1. <u>https://en.wikipedia.org/wiki/Mathematical\_finance.</u>
- 2. <u>onlinelibrary.wiley.com > Mathematics > Business & Finance</u>
- 3. <u>https://www.coursera.org/course/mathematicalmethods</u>
- 4. <u>https://plus.maths.org/content/what-financial-mathematics</u>



## FACULTY OF SCIENCES

## **DEPARTMENT OF MATHEMATICS**

#### COURSE: B.Sc. SUBJECT NAME: Mathematics Practical-IV Teaching & Evaluation Scheme:-

SEMESTER: IV SUBJECT CODE: 4SC04MAP1

| Теа | ching | hours | /week | Credit | Evaluation Scheme/semester                 |     |            |                |    |        |     |     |
|-----|-------|-------|-------|--------|--|-----|------------|----------------|----|--------|-----|-----|
|     |       |       |       |        | Theory                                     |     |            |                |    | Practi | cal |     |
| Th  | Tu    | Pr    | Total |        | Sessional University<br>Exam Exam Internal |     | University | Total<br>Marks |    |        |     |     |
|     |       |       |       |        | Marks                                      | Hrs | Marks      | Hrs            | Pr | TW     |     |     |
| 0   | 0     | 6     | 6     | 3      |  |     |            |                | 20 | 10     | 70  | 100 |

**Objectives: -** The main objectives of this course are

- To solve algebraic and transcendental equation by using different methods
- Use integration to find area of region and volume of surface.

#### **Prerequisites:-**

Basic knowledge of differentiation, integration, calculus and differential equations.

| Sr. | Course Contents   |
|-----|---|
| No. |   |
| 1   | Problems based on first order partial differential equation, formation of partial       |
|     | differential equation.  |
| 2   | Problems based on gradient, divergence & curl of vector in $R^3$ .                      |
| 3   | Problems based on double integral, Triple integral, Change of variable in multiple      |
|     | integral.   |
| 4   | Problems based on line integral, surface integral, Green's theorem, Gauss – Divergence  |
|     | theorem, Stoke's theorem.   |
| 5   | Problems based on angles between two curves, radius of curvature for Cartesian,         |
|     | parametric and polar equations, arc length of the curves given in Cartesian, parametric |
|     | and polar forms   |
| 6   | Problems based on orthogonalization, angles, Gram schmidth orthogonalisation process.   |



| 7  | Problems based on geometric applications orthogonal linear transformation.  |
|----|---|
| 8  | Problems based on determinant, diagonalization of symmetric matrices, canonical form of conics and quadratics.                              |
| 9  | Problems based on bisection method, method of iteration, Newton – Raphson formula, Newton's iterative formula and method of false position. |
| 10 | Problems based on Trapezoidal rule, Simpson's $\frac{1}{3}$ rule, Simpson's $\frac{3}{8}$ rule, Weddle's rule,                              |
|    | Taylor's series method, Picard's method, Euler's Method, Runge – Kutta method.  |
|    | OR  |
| 9  | Problems based on mathematical finance.   |
| 10 | Problems based on mathematical finance.   |

#### Learning Outcomes:-

After successful completion of this course student will be able to

- Solve any problem related to differential or integral calculus.
- Analyze errors and have an understanding of error estimation.
- Be able to use polynomials in several ways to approximate both function and data, and to much the type of polynomial approximation to a given type of problem.
- Be able to solve equations in one unknown real variable using iterative methods and to understand how long these methods take to converge to a solution.
- Derive formulas to approximate the derivative of a function at a point and formulas to compute the definite integral of a function of one or more variables.
- Choose and apply any of several modern methods for solving systems of initial value problems based on properties of the problem.

#### **Books Recommended:-**

- 1. 'Numerical Analysis and Computational Procedures', **S. A. Moolah**, New Central Book Agency (P) Ltd., Calcutta.
- 2. 'Elementary Numerical analysis', S. S. Sastry, Prentice Hall, New Delhi.
- 3. 'Advanced Calculus', David Widder, Prentice hall, New Delhi.
- 4. 'Advanced Calculus Volume-II, T. M. Apostol, Blaisdoll.
- 5. 'Differential Calculus', Shanti Narayan & P. K. Mittal, S. Chand.
- 6. 'Integral Calculus', Shanti Narayan & P. K. Mittal, S. Chand.
- 7. 'Partial Differential Equation', **T. Amarnath**, *Narosa*.
- 8. 'Linear Algebra A Geometric Approach', S. Kumaresan, Prentice Hall, New Delhi.
- 9. 'Finite Dimensional Vector spaces', P. Halmos, Literary Licensing, LLC.
- 10. 'Matrix and Linear algebra', K. B. Dutta, Prentice Hall, New Delhi.
- 11. 'Linear Algebra-A problem book', **P. R. Halmos,** *Cambridge university Press.*

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- 12. 'Investment Science', D. G. Luenberger, Oxford University Press, Delhi, 1998.
- 13. 'Options, Futures and Other Derivatives', J. C. Hull, Prentice-Hall India, Indian reprint, 2006.
- 14. 'An Elementary Introduction to Mathematical Finance', **S. Ross,** *Cambridge University Press, USA, 2003*

#### Notes:-

- 1. Problem solving skill in mathematics is an important aspect in the teaching of mathematics.
- 2. There would be problem solving session of six hours per week and they will be conducted in batches.